#### Homework question: Implement a neural network to *distinguish\** low-quality characters



MCB111 Section week 8 Nicolas Gort Freitas 10/28/2022

## Implementation options



- Classification using a one-neuron network (i.e. a perceptron)
- Reconstruction using a Hopfield network

# Hopfield networks are recurrent networks that don't use backpropagation to learn



#### Hopfield Network (HN)



Recurrent networks include cycles in their topology

Some, like LSTMs, do apply backpropagation

Hopfield networks, on the other hand uses something

Source: asimovinstitute.org

## Hopfield networks are fully connected graphs with symmetrical weights



The weights are usually packed together in a matrix With N rows and N columns, where N is the number of neurons

$$\mathbf{W} \in \mathbb{R}^{N \times N}$$

Self-edges have weight 0 by definition.

$$w_{n,n} = 0$$

Weights are symmetrical for any pair of neurons m, n:

$$W_{m,n} = W_{n,m}$$

#### Hopfield networks are modeled after associative memory



This principle, called Hebbian learning, postulates that it is most efficient for neurons to strengthen synapses among neurons that tend to fire in the same situations.

## Hopfield networks interpret training observations in terms of their pairwise relationships



#### Training on multiple patterns



W trained on "A"



W trained on "B"







W trained on "C"





## **Training on multiple patterns**

Simply add up the results from each observation!



W trained on "A"



W trained on "B"



W trained on "C"



$$w_{m,n} = \sum_{i}^{K} y_m^{(i)} \cdot y_n^{(i)}$$

Here m and n are features of each flattened observation, K is the number of observations

W trained on "A" and "B"



W trained on "A", "B", and "C"







#### So far we've covered how Hopfield networks can be trained...



W

## But how will they aid us in our task to recognize corrupted representations?



# Image reconstruction is performed through iterative updates based on train weights

- 1. Update each element / pixel based on trained weights
- 2. Repeat until convergence
- 3. Check whether it matches one of the trained patterns?

$$\tilde{y}_n \leftarrow \begin{cases} +1 & \text{if } \sum_m w_{m,n} y_n \ge 0\\ -1 & \text{otherwise} \end{cases}$$

$$\mathbf{y} \to \tilde{\mathbf{y}}^{(1)} \to \dots \to \tilde{\mathbf{y}}^{(\infty)}$$



## **Final reflection questions**

- Why does a Hopfield network reflect the principle of "fire together, wire together"?
- Many neuroscientists believe memories are in synapses rather than neurons. How would a Hopfield network relate to this model of memory?
- When updating our y's, will we always converge to one of the elements in the training set?
- Can you unlearn a memory in a Hopfield network? How would you envision this happening?